

Modulation Techniques for Mobile Radio

- Modulation is the process of encoding information from message source in a manner suitable for transmission.
- It generally involves translating a base band message signal (source) to a bandpass signal at frequencies \gg baseband frequency.
- Demodulation is the process of extracting the baseband message from the carrier.

Modulation

Analog Modulation

Digital Modulation techniques

- First Generation mobile radio Present & future systems

Review of Analog modulation Schemes

Amplitude Modulation

- $m(t)$ – message signal
- $A_c \cos (2\pi f_c t)$ - Carrier signal
- AM Signal $S_{AM}(t) = A_c [1+m(t)] \cos (2\pi f_c t)$
- AM Spectrum

$$S_{AM}(f) = 0.5 A_c [\delta(f - f_c) + m(f - f_c) + \delta(f + f_c) + m(f + f_c)]$$

AM parameters

- Modulation Index $k = A_m / A_c \leq 1$

- Bandwidth $B_{AM} = 2 f_m$

- Total Power in AM signal

$$P_{AM} = 0.5 A_c^2 [1 + 2\langle m(t) \rangle + \langle m^2(t) \rangle]$$

- Power in the carrier $P_c = A_c^2 / 2$

Single Sideband AM

Signal $S_{SSB} = A_c [m(t)\cos(2\pi f_c t) \pm m(t)\sin(2\pi f_c t)]$

lower sideband \wedge

upper sideband

\wedge

- $m(t) = m(t) \otimes h(t)$

$$h(t) = 1/\pi t$$

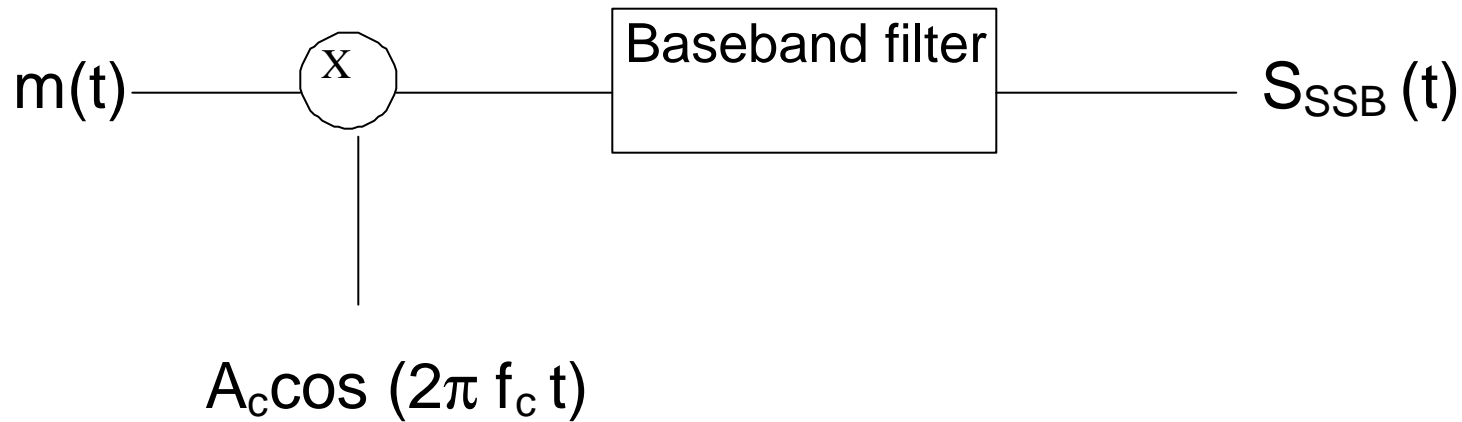
- Hilbert transform of $m(t)$

$$H(f) = -j, f > 0$$

$$H(f) = +j, f < 0$$

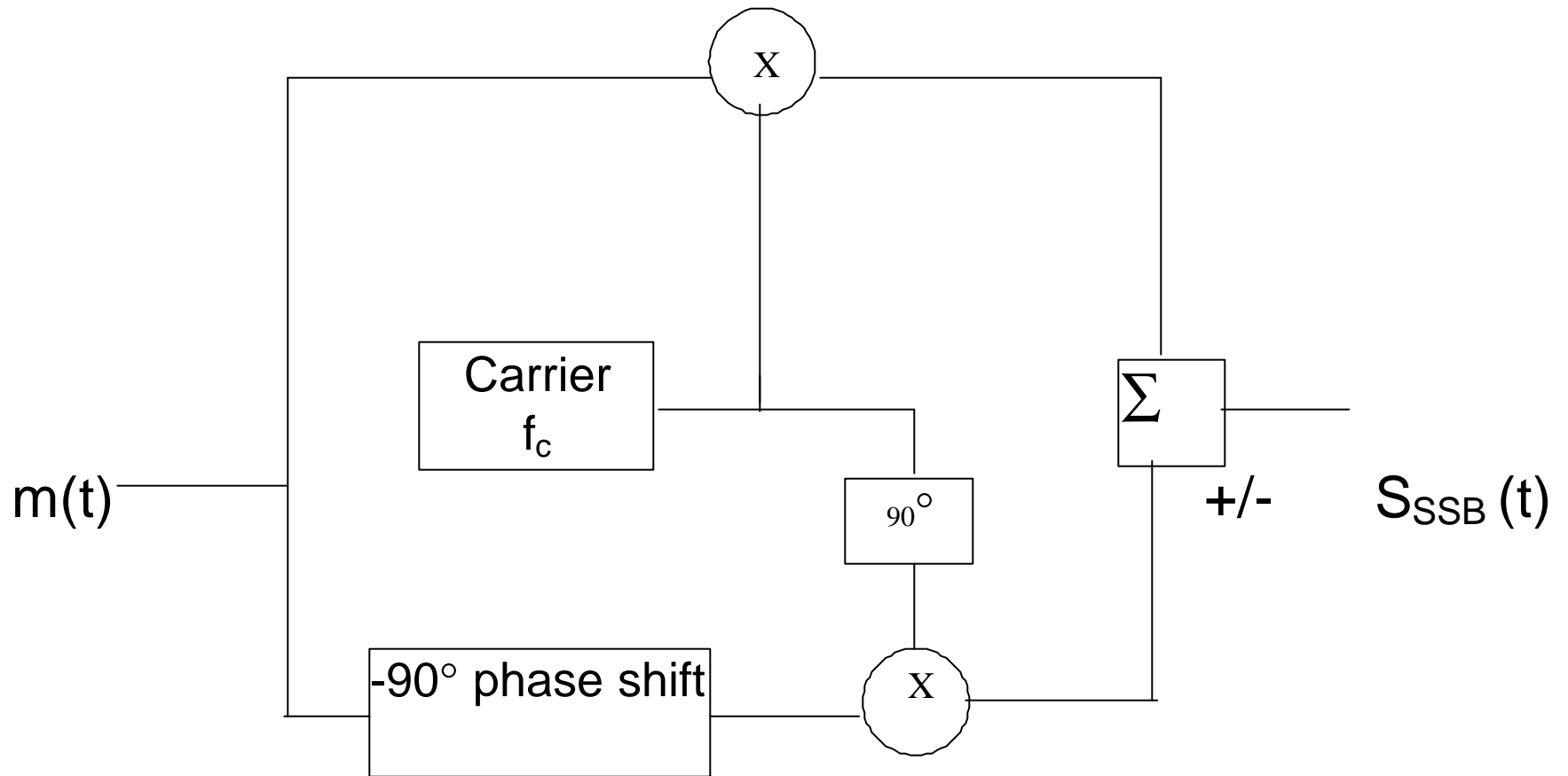
SSB Generation

Filter Method



- Baseband filter passes only one of the sidebands- upper or lower

Balanced Modulator



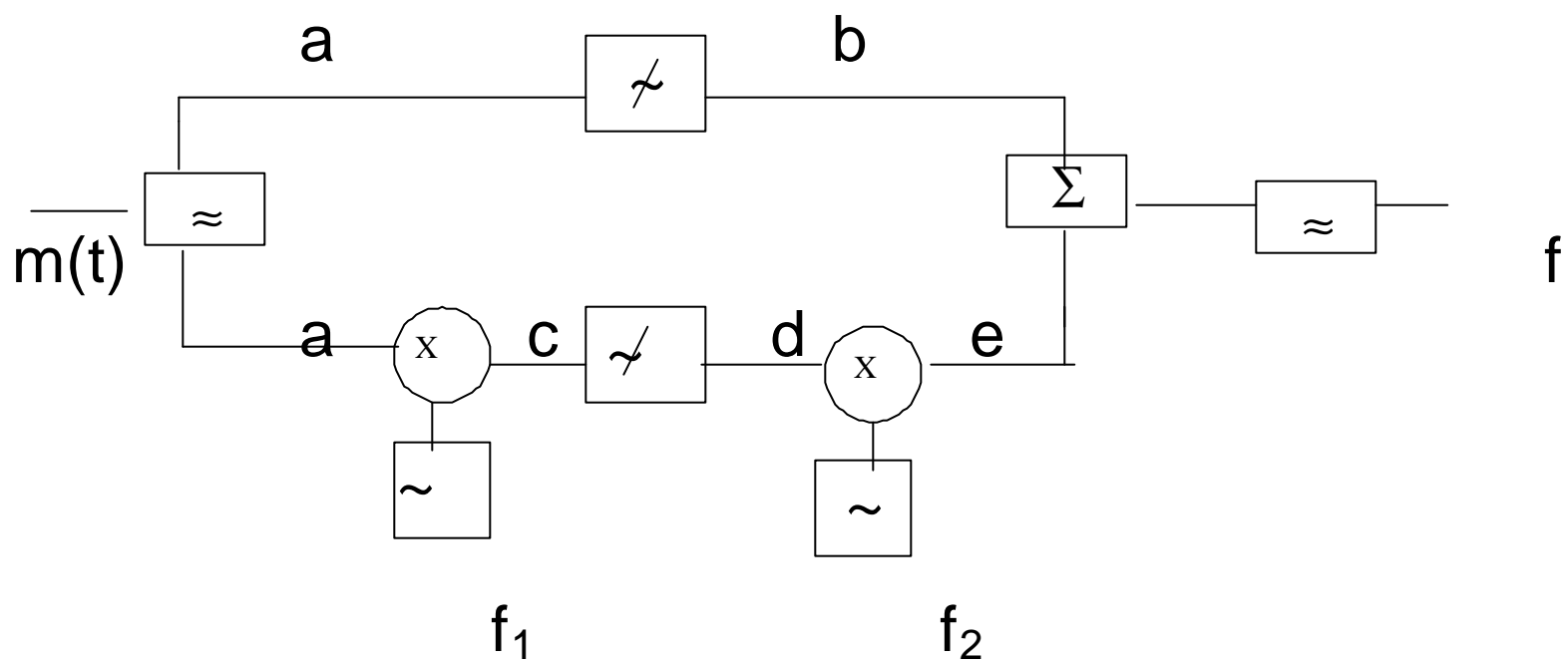
Properties of SSB

- Bandwidth = f_m
- Bandwidth of SSB is very efficient
- However, Doppler spreading and Rayleigh fading can shift the signal spectrum, causing distortion.
- Frequency of the receiver oscillator must be exactly the same as that of the transmitted carrier f_c . If not, this results in a frequency shift $f_c \pm \Delta f$, causes distortion.

Solution - Pilot Tone SSB

- Transmit a low level pilot tone along with the SSB signal
- The pilot tone has information on the frequency and amplitude of the carrier.
- The pilot tone can be tracked using signal processing
FFSR - Feed Forward Signal Regeneration.
- Keeping the phase and amplitude of the pilot as reference, the phase and amplitude distortion in the received sidebands can be corrected.

TTIB (Transparent Tone In-Band) System



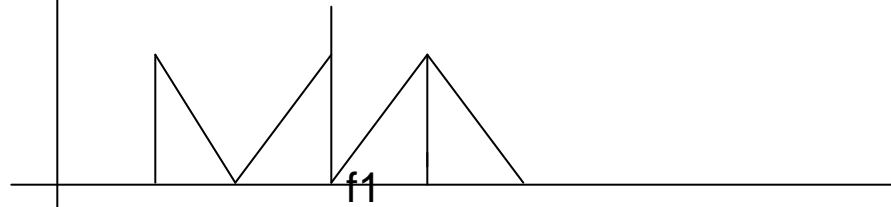
a



b



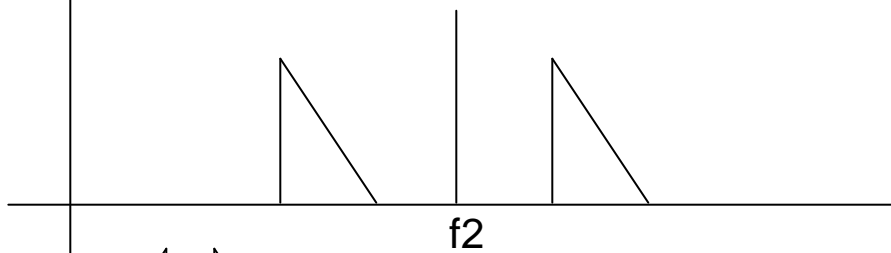
c



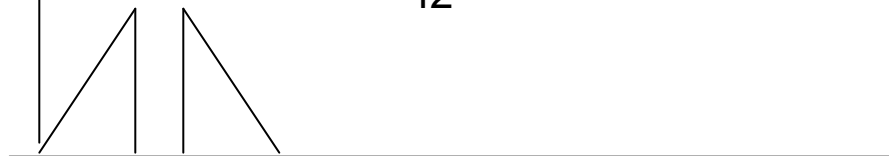
d



e



f



$$BW = f_2 - f_1$$

frequency

Properties of TTIB system

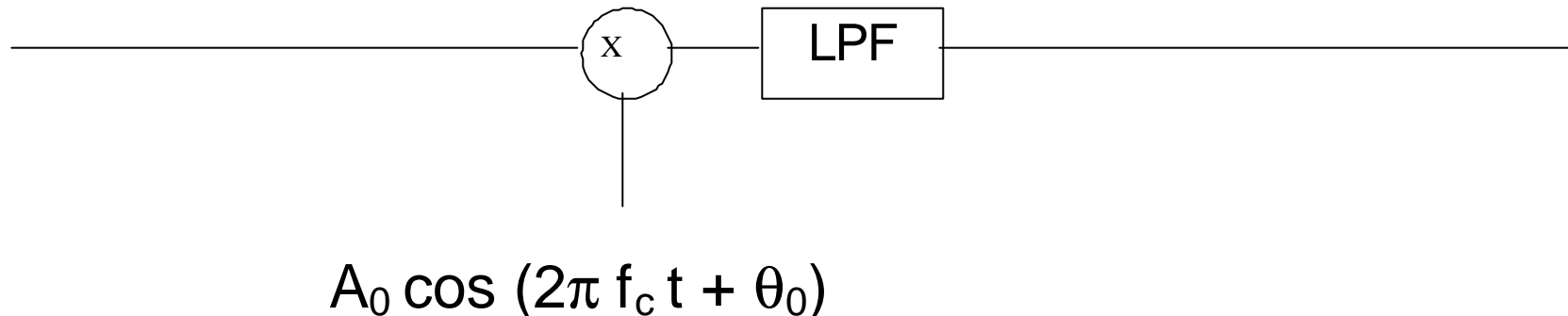
- Tone frequency is transparent to data => avoids overlap with audio frequency
- Baseband signal is split into two equal width segments
- Small portion of audio spectrum is removed and a low-level pilot tone is inserted in its place.
- This procedure maintains the low bandwidth of the SSB signal
- Provides good adjacent channel protection

Demodulation of AM signals

Coherent Demodulation

$$S_{AM} = R(t) \cos(2\pi f_c t + \theta_r)$$

$$V_{OUT}(t) = 0.5 A_0 R(t) \cos(\theta_r - \theta_0)$$



- Coherent demodulation requires knowledge of the transmitted carrier frequency and phase at the receiver.

Non-coherent Demodulation

Envelope Detectors

Frequency Modulation

- Message signal $m(t)$
- FM signal

$$S_{FM}(t) = A_c \cos\left[2\pi f_c t + 2\pi k_f \int_{-\infty}^t m(t) dt\right]$$

- Power in FM signal $P_{FM} = A_c^2 / 2$
- Frequency modulation index $\beta_f = k_f A_M / W = \Delta f / W$

W = Highest frequency component in message signal $m(t)$

A_M = Peak value of modulating signal $m(t)$

Phase Modulation

- PM signal $S_{PM}(t) = A_c \cos[2\pi f_c t + k_\theta m(t)]$
- Phase modulation index $\beta_\theta = k_\theta A_M$
- Power in PM signal: $P_{PM} = A_c^2 / 2$

Bandwidth $B_T = 2\Delta f$

FM modulation/demodulation methods

FM Modulation

- Direct Method – VCO
- Indirect Method – Armstrong

FM Detection

- Slope Detection
- Zero Crossing Detection
- PLL for FM Detection
- Quadrature Detection

Comparison between AM and FM

FM	AM
<ul style="list-style-type: none">• FM signals are less susceptible to atmospheric noise, because information is stored as frequency variations rather than amplitude variations.	<ul style="list-style-type: none">• AM signals are more susceptible to noise, because information is stored as amplitude variations rather than frequency variations.
<ul style="list-style-type: none">• The modulation index can be varied to obtain greater SNR (6dB for each doubling in bandwidth)	<ul style="list-style-type: none">• Modulation index cannot be changed automatically.
<ul style="list-style-type: none">• FM signals occupy more bandwidth	<ul style="list-style-type: none">• AM signals occupy lesser bandwidth.
<ul style="list-style-type: none">• Efficient Class C amplifiers	<ul style="list-style-type: none">• Class A or AB amplifiers

Trade off between SNR and Bandwidth in an FM signal

- SNR at output of a properly designed FM receiver is

$$(\text{SNR})_{\text{out}} = 6(\beta_f + 1) \beta_f^2 \overline{(m(t)^2 / A_M)} (\text{SNR})_{\text{in}}$$

- $(\text{SNR})_{\text{in}} = [A_c^2 / 2] / [2N_0(\beta_f + 1)B]$

N_0 = White noise RF power spectral density

B = Equivalent RF bandwidth of BP filter at front end of receiver

Example: For $m(t) = A_m \sin(\omega_m t)$

$$(\text{SNR})_{\text{out}} / (\text{SNR})_{\text{in}} = 3\beta_f^2(\beta_f + 1)$$

Digital Modulation

- Advancements in VLSI and DSP have made digital modulation more cost efficient than analog transmission systems.
- **Advantages**
 - Greater noise immunity
 - Easier multiplexing of information (voice, data, video)
 - Can accommodate digital transmission errors, source coding, encryption and equalization.
 - DSP can implement digital modulators, demodulators completely in software.

Basics of digital communications

- In digital wireless communication systems, the message (modulating signal) is represented as a time sequence of symbols or pulses.
- Each symbol has m finite states
Example $m=8$
Each symbol represents n bits of information
 $n = \log_2 m \text{ bits/symbol} = 3$

Bandwidth efficiency and Shannon's capacity theorem

- **Bandwidth efficiency** $\eta_B = R / B$ bps/Hz

R=Data rate in bits/second

B=Bandwidth occupied by modulated RF signal

- **Shannon's formula**

$$\eta_{B_{\max}} = C/B = \frac{\text{channel capacity (bits/s)}}{\text{RF bandwidth}}$$

$$= \log_2(1 + S/N)$$

S/N = Signal to noise ratio

Example : For US digital cellular standard, R = 48.6 kbps

RF bandwidth = 30 khz

For SNR = 20 dB = 100

$$C = 30000 * \log_2(1 + S/N)$$

$$= 30000 * \log_2(1 + 100) = 199.75 \text{ kbps}$$

For GSM standard R = 270.833 kbps

$$C = 1.99 \text{ Mbps for } S/N = 30 \text{ dB}$$

Bandwidth and Power Spectral density(PSD) of Digital signals

Power Spectral density (PSD) of a random signal $w(t)$ is defined as:

$$P_w(f) = \lim_{T \rightarrow \infty} \frac{\overline{|W_T(f)|^2}}{T}$$

$$w_T(t) \longleftrightarrow W_T(f)$$

$$w_T(t) = w(t) \quad , \quad -T/2 < t < T/2$$
$$= 0 \quad , \quad \text{elsewhere}$$

PSD of modulated signal

$$s(t) = \text{Re} \{ g(t) e^{j2\pi f_c t} \}$$

$$P_s(f) = .25 [P_g(f - f_c) + P_g(f + f_c)]$$

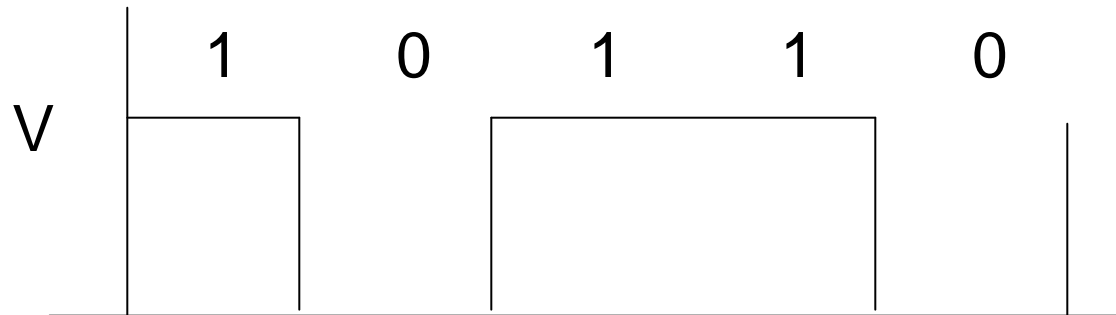
Bandwidth

- Absolute Bandwidth
- Null-to-null bandwidth
- Half Power bandwidth (3 dB bandwidth)

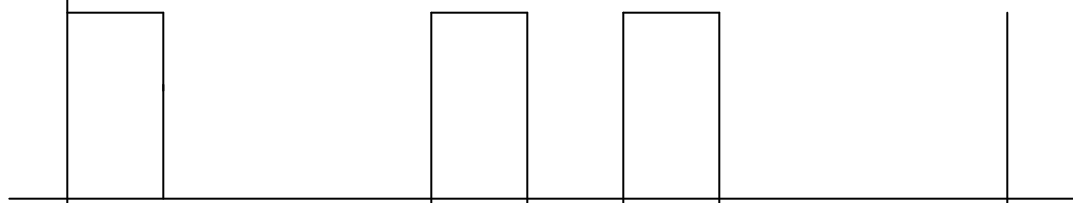
Line Coding

- Line codes are used to provide particular spectral characteristics of a pulse train.
- Most commonly used
 - ◇ Return-to-zero (RZ)
 - ◇ Nonreturn-to-zero (NRZ)
 - ◇ Manchester Code
- Unipolar (0, V) or Bipolar (-V, V)

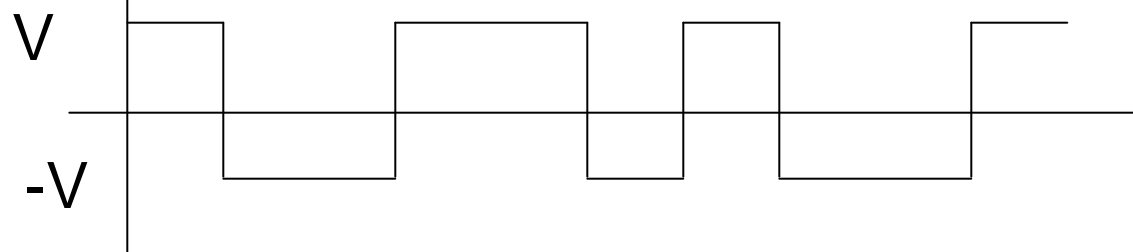
Unipolar



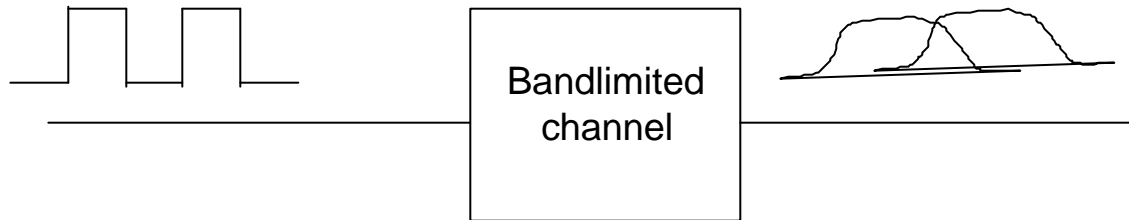
RZ



Manchester
NRZ



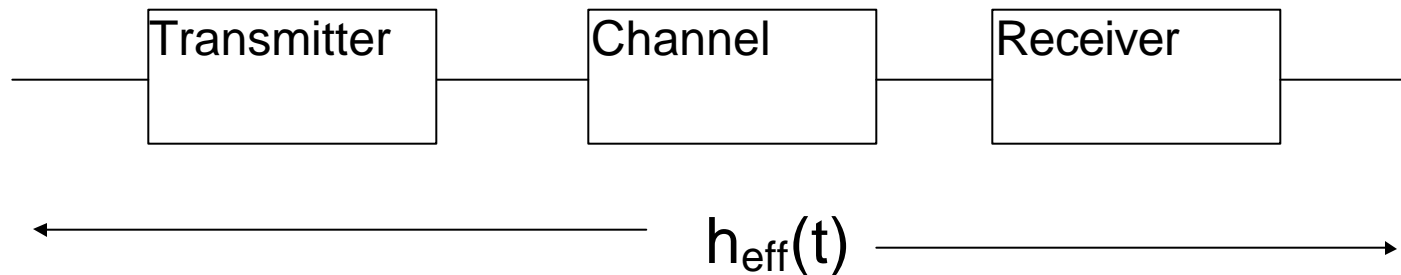
Pulse Shaping Techniques



- ISI – Inter symbol interference
⇒ errors in transmission of symbols
- Pulse shaping techniques → reduces the intersymbol effects

Nyquist criteria for ISI cancellation

Condition for impulse response for overall communication system



$$h_{\text{eff}}(nT_s) = k \text{ (constant)}, \quad n = 0$$
$$= 0, \quad n \neq 0$$

T_s = symbol period

k = non zero constant

